

# Lab8 : FE and DID

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# Section 1

## FE in Stata

## Subsection 1

### Panel Data

- Panel Data

- ▶ Panel data refers to data with observations on **multiple entities**, where each entity is observed at **two or more points in time**.
- ▶ We focus on **balanced** and **micro** panel data.
- ▶ **Balanced** panel: each unit of observation  $i$  is observed the same number of time periods,  $T$ .
- ▶ **Micro** : large  $N$ , and small  $T$ , more similar to cross-section data.

## Subsection 2

### Review the Theory

- Review the Theory

- ▶ Fixed effects regression is a method for **controlling for omitted variables** in panel data when the omitted variables **vary across entities (states)** but do **not change over time**.
- ▶ Specification :

$$Y_{it} = \beta_0 + \beta_1 X_{it} + \beta_2 Z_i + u_{it} \quad (11.1)$$

- Because  $Z_i$  varies from one state to the next but is constant over time, then let  $\alpha_i = \beta_0 + \beta_2 Z_i$ , the Equation becomes

$$Y_{it} = \beta_1 X_{it} + \alpha_i + u_{it} \quad (11.2)$$

- This is the **fixed effects regression model**, in which  $\alpha_i$  are treated as *unknown intercepts* to be estimated, one for each state. The interpretation of  $\alpha_i$  as a *state-specific intercept* in Equation (11.2).
- Arbitrarily omit the binary variable  $D1_i$  for the first group. Accordingly, the fixed effects regression model in Equation (7.2) can be written equivalently as

$$Y_{it} = \beta_0 + \beta_1 X_{it} + \gamma_2 D2_i + \gamma_3 D3_i + \dots + \gamma_n Dn_i + u_{it} \quad (7.3)$$

- Review the Theory

- ▶ Estimation:

- entity-demeaned :

$$\hat{\beta}_{demean} = \frac{\sum_{i=1}^n \sum_{t=1}^T \tilde{Y}_{it} \tilde{X}_{it}}{\sum_{i=1}^n \sum_{t=1}^T \tilde{X}_{it}^2}$$

- first-difference estimator :

$$\hat{\beta}_{fd} = \frac{\sum_{i=1}^n \sum_{t=2}^T \Delta Y_{it} \Delta X_{it}}{\sum_{i=1}^n \sum_{t=2}^T \Delta X_{it}^2}$$

## • Summary

- ▶ FE 实质上就是在传统的线性回归模型中加入  $N-1$  个虚拟变量;
- ▶ 使得每个截面都有自己的截距项, 截距项的不同反映了个体的某些不随时间改变的特征;
- ▶ 我们关注的是  $X$  的系数, 而非每个截面的截距项。



## Subsection 3

### Examples for FE

- Examples for FE
  - ▶ unbalance —> balance

```
. use abond.dta, clear
. xtset id year
    panel variable:  id (unbalanced)
    time variable:  year, 1976 to 1984
                  delta:  1 unit
```

# FE in Stata

- Examples for FE

► unbalance —> balance

```
. xtides      /*unbalanced*/
      id:  1, 2, ..., 140          n =      140
      year: 1976, 1977, ..., 1984  T =        9
      Delta(year) = 1 unit
      Span(year)  = 9 periods
      (id*year uniquely identifies each observation)
```

Distribution of T\_i:

	min	5%	25%	50%	75%	95%	max
	7	7	7	7	8	9	9

Freq.	Percent	Cum.	Pattern
62	44.29	44.29	1111111..
39	27.86	72.14	.1111111.
19	13.57	85.71	.11111111
14	10.00	95.71	111111111
4	2.86	98.57	11111111.
2	1.43	100.00	..1111111
140	100.00		XXXXXXXXX

# FE in Stata

- Examples for FE

► unbalance —> balance

```
. sum      /*many missing values*/
```

Variable	Obs	Mean	Std. Dev.	Min	Max
c1	0				
ind	1,031	5.123181	2.678095	1	9
year	1,031	1979.651	2.21607	1976	1984
emp	1,031	7.891677	15.93492	.104	108.562
wage	1,031	23.9188	5.648418	8.0171	45.2318
cap	1,031	2.507432	6.248712	.0119	47.1079
indoutpt	1,031	103.8012	9.938008	86.9	128.3653
n	1,031	1.056002	1.341506	-2.263364	4.687321
w	1,031	3.142988	.2630081	2.081577	3.8118
k	1,031	-.4415775	1.514132	-4.431217	3.852441
ys	1,031	4.638015	.0939611	4.464758	4.85488
rec	1,031	516	297.7684	1	1031
yearm1	1,031	1979.644	2.213454	1976	1984
id	1,031	73.20369	41.23333	1	140
nL1	891	1.083518	1.338469	-2.095571	4.687321
nL2	751	1.107716	1.333478	-2.079442	4.687321
wL1	891	3.132166	.2639638	2.081577	3.8118
kL1	891	-.4131872	1.501461	-4.431217	3.852441
kL2	751	-.392113	1.486371	-4.431217	3.852441
ysL1	891	4.651039	.0923352	4.464758	4.85488

- Examples for FE

► unbalance —> balance

```
. xtbalance, rang(1978 1982) miss(_all)    /*written by arlion*/
(331 observations deleted due to out of range)
(62 observations deleted due to missing)
(238 observations deleted due to discontinues)
. xtides
      id:  5, 6, ..., 140                      n =          80
     year: 1978, 1979, ..., 1982                T =           5
           Delta(year) = 1 unit
           Span(year)  = 5 periods
           (id*year uniquely identifies each observation)

Distribution of T_i:  min      5%      25%      50%      75%      95%      max
                    5         5         5         5         5         5

```

Freq.	Percent	Cum.	Pattern
80	100.00	100.00	11111
80	100.00		XXXXX

- Examples for FE

- ▶ Data : Baum(2006)

- ▶ 包含美国 48 个州 1982-1988 年交通死亡率相关变量:

- fatal (交通死亡率)

- beertax (啤酒税)

- spircons (酒精消费量)

- unrate (失业率)

- perinck (人均收入, 千元)

- state (州)

- year (年)

- Examples for FE

- ▶ Pooled OLS & Pooled OLS with Time (Wrong)

```
. use traffic, clear
. est clear
. eststo : qui reg fatal beertax
(est1 stored)
. eststo : qui reg fatal beertax i.year
(est2 stored)

. esttab, star(* .1 ** .05 * .01)    ///
      nogap nonumber replace         ///
      se(%5.4f) ar2
```

# FE in Stata

- Examples for FE

- ▶ Pooled OLS & Pooled OLS with Time (Wrong)

	fatal	fatal
beertax	0.365* (0.0622)	0.366* (0.0626)
1982.year		0 (.)
1983.year		-0.0820 (0.1117)
1984.year		-0.0717 (0.1117)
1985.year		-0.111 (0.1117)
1986.year		-0.0161 (0.1117)
1987.year		-0.0155 (0.1117)
1988.year		-0.00103 (0.1117)
_cons	1.853* (0.0436)	1.895* (0.0857)
N	336	336
adj. R-sq	0.091	0.079

Standard errors in parentheses

\* p<.1, \*\* p<.05, \* p<.01



- Examples for FE

- ▶ Fixed effects regression

```
. xtset state year //设定state与year为面板（个体）变量及时间变量
      panel variable:  state (strongly balanced)
      time variable:  year, 1982 to 1988
              delta:  1 unit

. xtodes
      state:  1, 4, ..., 56                      n =          48
      year:  1982, 1983, ..., 1988                T =           7
              Delta(year) = 1 unit
              Span(year)  = 7 periods
              (state*year uniquely identifies each observation)

Distribution of T_i:  min    5%    25%    50%    75%    95%    max
                   7      7      7      7      7      7      7

      Freq.  Percent   Cum. | Pattern
      -----|-----
      48     100.00  100.00 | 1111111
      48     100.00      .   | XXXXXXX
```

# FE in Stata

- Examples for FE

- Fixed effects regression

. xtsum fatal beertax spircons unrates perinck state year							
Variable		Mean	Std. Dev.	Min	Max	Observations	
fatal	overall	2.040444	.5701938	.82121	4.21784	N =	336
	between		.5461407	1.110077	3.653197	n =	48
	within		.1794253	1.45556	2.962664	T =	7
beertax	overall	.513256	.4778442	.0433109	2.720764	N =	336
	between		.4789513	.0481679	2.440507	n =	48
	within		.0552203	.1415352	.7935126	T =	7
spircons	overall	1.75369	.6835745	.79	4.9	N =	336
	between		.6734649	.8614286	4.388572	n =	48
	within		.147792	1.255119	2.265119	T =	7
unrates	overall	7.346726	2.533405	2.4	18	N =	336
	between		1.953377	4.1	13.2	n =	48
	within		1.634257	4.046726	12.14673	T =	7
perinck	overall	13.88018	2.253046	9.513762	22.19345	N =	336
	between		2.122712	9.95087	19.51582	n =	48
	within		.8068546	11.43261	16.55782	T =	7
state	overall	30.1875	15.30985	1	56	N =	336
	between		15.44883	1	56	n =	48
	within		0	30.1875	30.1875	T =	7

# FE in Stata

- Examples for FE

- Fixed effects regression

```
. xtline fatal if year==1982  
. graph export fefig1.png,width(500) replace  
(file fefig1.png written in PNG format)
```



# FE in Stata

- Examples for FE

- ▶ Fixed effects regression

```
. xtreg fatal beertax spircons unrates perinck, fe
Fixed-effects (within) regression              Number of obs   =       336
Group variable: state                        Number of groups =       48
R-sq:                                         Obs per group:
    within = 0.3526                           min =           7
    between = 0.1146                          avg =          7.0
    overall = 0.0863                          max =           7
                                         F(4,284)        =      38.68
corr(u_i, Xb) = -0.8804                      Prob > F         =      0.0000
```

fatal	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
beertax	-.4840728	.1625106	-2.98	0.003	-.8039508	-.1641948
spircons	.8169652	.0792118	10.31	0.000	.6610484	.9728819
unrates	-.0290499	.0090274	-3.22	0.001	-.0468191	-.0112808
perinck	.1047103	.0205986	5.08	0.000	.064165	.1452555
_cons	-.383783	.4201781	-0.91	0.362	-1.210841	.4432754
sigma_u	1.1181913					
sigma_e	.15678965					
rho	.98071823	(fraction of variance due to u_i)				

```
F test that all u_i=0: F(47, 284) = 59.77                      Prob > F = 0.0000
. est store FE
```

# FE in Stata

- Examples for FE

- ▶ Fixed effects regression
- ▶ clustered standard errors

```
. xtreg fatal beertax spircons unrates perinck, fe vce(cluster state)
Fixed-effects (within) regression      Number of obs   =       336
Group variable: state                 Number of groups =       48
R-sq:                                Obs per group:
    within = 0.3526                      min =          7
    between = 0.1146                     avg =         7.0
    overall = 0.0863                      max =          7
                                         F(4,47)         =      21.27
corr(u_i, Xb) = -0.8804                 Prob > F         =      0.0000
                                         (Std. Err. adjusted for 48 clusters in state)
```

fatal	Robust					
	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
beertax	-.4840728	.2218754	-2.18	0.034	-.9304285	-.037717
spircons	.8169652	.1272627	6.42	0.000	.5609456	1.072985
unrates	-.0290499	.0094581	-3.07	0.004	-.0480772	-.0100227
perinck	.1047103	.0341455	3.07	0.004	.0360184	.1734022
_cons	-.383783	.7091738	-0.54	0.591	-1.810457	1.042891
sigma_u	1.1181913					
sigma_e	.15678965					
rho	.98071823	(fraction of variance due to u_i)				

```
. est store FE_cse
```

# FE in Stata

- Examples for FE

- ▶ Fixed effects regression
- ▶ Both Entity and Time Fixed Effects

```
. xtreg fatal beertax spircons unrates perinck i.year, fe vce(cluster state)
Fixed-effects (within) regression              Number of obs   =        336
Group variable: state                        Number of groups =         48
R-sq:                                         Obs per group:
    within = 0.4528                          min =           7
    between = 0.1090                         avg =          7.0
    overall  = 0.0770                        max =           7
                                           F(10,47)        =       14.13
corr(u_i, Xb) = -0.8728                      Prob > F         =       0.0000
                                           (Std. Err. adjusted for 48 clusters in state)
```

fatal	Robust					
	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
beertax	-.4347195	.2442775	-1.78	0.082	-.9261425	.0567036
spircons	.805857	.1161087	6.94	0.000	.5722764	1.039438
unrates	-.0549084	.011763	-4.67	0.000	-.0785725	-.0312443
perinck	.0882636	.0322971	2.73	0.009	.0232901	.153237
year						
1983	-.0533713	.0312438	-1.71	0.094	-.1162256	.0094831
1984	-.1649828	.0439375	-3.75	0.000	-.2533737	-.076592
1985	-.1997376	.0496167	-4.03	0.000	-.2995535	-.0999218
1986	-.0508034	.0661756	-0.77	0.447	-.1839315	.0823248
1987	-.1000728	.0756768	-1.32	0.192	-.2523149	.0521693

# FE in Stata

- Examples for FE

- Fixed effects regression

```
. esttab FE FE_cse FE_TW, star(* .1 ** .05 * .01) ///  
> nogap nonumber replace se(%5.4f) ar2 drop(1982.year)
```

	fatal	fatal	fatal
beertax	-0.484* (0.1625)	-0.484** (0.2219)	-0.435* (0.2443)
spircons	0.817* (0.0792)	0.817* (0.1273)	0.806* (0.1161)
unrate	-0.0290* (0.0090)	-0.0290* (0.0095)	-0.0549* (0.0118)
perinck	0.105* (0.0206)	0.105* (0.0341)	0.0883* (0.0323)
1983.year			-0.0534* (0.0312)
1984.year			-0.165* (0.0439)
1985.year			-0.200* (0.0496)
1986.year			-0.0508 (0.0662)
1987.year			-0.100 (0.0757)
1988.year			-0.134 (0.0864)
_cons	-0.384 (0.4202)	-0.384 (0.7092)	0.129 (0.6238)
N	336	336	336
adj. R-sq	0.236	0.345	0.436

Standard errors in parentheses  
\* p<.1, \*\* p<.05, \* p<.01

## Section 2

### DID in Stata



## Subsection 1

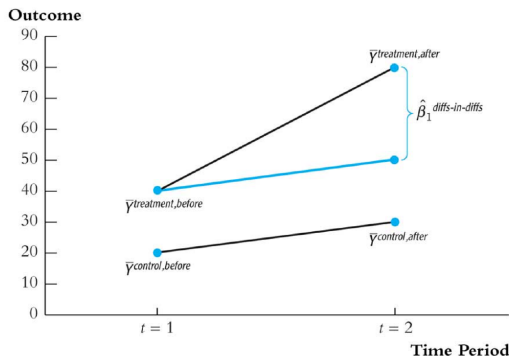
### Review the Theory

- Review the Theory

## DID estimator

- The DID estimator is

$$\hat{\beta}_{DID} = (\bar{Y}_{treat,post} - \bar{Y}_{treat,pre}) - (\bar{Y}_{control,post} - \bar{Y}_{control,pre})$$



- Review the Theory

Difference in Differences

Card and Krueger(1994): Minimum Wage on Employment

## Regression DD - Card and Krueger

- A  $2 \times 2$  matrix table

		treat or control	
		NJ=0(control)	NJ=1(treat)
pre or post	d=0(pre)	$\alpha$	$\alpha + \gamma$
	d=1(post)	$\alpha + \lambda$	$\alpha + \gamma + \lambda + \delta$

- Then DID estimator

$$\begin{aligned}
 \hat{\beta}_{DID} &= (\bar{Y}_{treat,post} - \bar{Y}_{treat,pre}) - \\
 &\quad (\bar{Y}_{control,post} - \bar{Y}_{control,pre}) \\
 &= (NJ_{post} - NJ_{pre}) - (PA_{post} - PA_{pre}) \\
 &= [(\alpha + \gamma + \lambda + \delta) - (\alpha + \gamma)] - [(\alpha + \lambda) - \alpha] \\
 &= \delta
 \end{aligned}$$

- Review the Theory

- ▶ Specification :

$$Y_{ist} = \alpha + \beta D_{st} + \gamma Treat_s + \delta Post_t + \Gamma X'_{ist} + u_{ist}$$

- Where  $D_{st}$  means  $(Treat \times Post)_{st}$
  - Using Fixed Effect Models further to transform into

$$Y_{ist} = \beta D_{st} + \alpha_s + \delta_t + \Gamma X'_{ist} + u_{ist}$$

- $\alpha_s$  is a set of groups fixed effects, which captures  $Treat_s$ .
      - $\delta_t$  is a set of time fixed effects, which captures  $Post_t$ .

## Subsection 2

### Examples for DID

- Examples for DID

- ▶ Data :

历史上 A、B、C、D、E、F、G 这 7 个地区非常相似

然而 1994 年后 E、F 和 G 三个地区 (treatment group) 颁布了一项政策

其余 4 个地区 (control group) 没有。

```
. use did, clear
```

## • Examples for DID

```
. * 假设政策执行时间为1994年，设置虚拟变量  
. gen time = (year>=1994) & !missing(year)  
  
. * 假设政策执行地为大于4的地方，设置虚拟变量  
. gen treated = (country>4) & !missing(country)  
  
. * 构建DID估计量，即时间和空间的交互项  
. gen did = time*treated
```

## • Examples for DID

```
. * DID <方法一>
. * 显然在10%水平上，政策实施有显著的负效应
. reg y did time treated, r
```

Linear regression

```
Number of obs   =      70
F(3, 66)        =      2.17
Prob > F        =     0.0998
R-squared       =     0.0827
Root MSE       =     3.0e+09
```

y	Coef.	Robust Std. Err.	t	P> t	[95% Conf. Interval]	
did	-2.52e+09	1.45e+09	-1.73	0.088	-5.42e+09	3.81e+08
time	2.29e+09	9.00e+08	2.54	0.013	4.92e+08	4.09e+09
treated	1.78e+09	1.05e+09	1.70	0.094	-3.11e+08	3.86e+09
_cons	3.58e+08	7.61e+08	0.47	0.640	-1.16e+09	1.88e+09

```
. * DID <方法二>
. qui reg y time##treated, r
```



# DID in Stata

## • Examples for DID

```
. * DID <方法三>
. * 与前两种方法结果一样

. *ssc install diff
. diff y, t(treated) p(time)
DIFFERENCE-IN-DIFFERENCES ESTIMATION RESULTS
Number of observations in the DIFF-IN-DIFF: 70
      Before      After
Control: 16      24      40
Treated: 12      18      30
       28      42
```

Outcome var.	y	S. Err.	t	P> t
Before				
Control	3.6e+08			
Treated	2.1e+09			
Diff (T-C)	1.8e+09	1.1e+09	1.58	0.120
After				
Control	2.6e+09			
Treated	1.9e+09			
Diff (T-C)	-7.4e+08	9.2e+08	0.81	0.422
Diff-in-Diff	-2.5e+09	1.5e+09	1.73	0.088*

R-square: 0.08  
\* Means and Standard Errors are estimated by linear regression  
\*\*Inference: \*\*\* p<0.01; \*\* p<0.05; \* p<0.1

- Examples for DID

- ▶ Test Paralled Trend

只有当地区在政策前足够相似才能够保证 DID 提取的是政策的因果效应；

因此，需要知道两组地区在政策前有多大差异；

生成年份虚拟变量  $\times$  实验组虚拟变量的交互项，捕捉两组地区在每一年份的差异；

如果两组地区的确有 Paralled Trend，那么预期在 1994 年前的那些交互项的回归结果将不显著，而 1994 年后的将显著。

- Examples for DID

- ▶ Test Paralled Trend

```
. *生成年份虚拟变量与实验组虚拟变量的交互项(此处选在政策前后各3年)
. gen Dyear = year-1994
. gen Before3 = (Dyear== -3 & treated==1)
. gen Before2 = (Dyear== -2 & treated==1)
. gen Before1 = (Dyear== -1 & treated==1)
. gen Current = (Dyear==0 & treated==1)
. gen After1 = (Dyear==1 & treated==1)
. gen After2 = (Dyear==2 & treated==1)
. gen After3 = (Dyear==3 & treated==1)
```

# DID in Stata

## • Examples for DID

### ► Test Paralled Trend

```
. * 将以上交互项作为解释变量进行回归
. * 可以看出Before3 Before2 Before1 的系数均不显著, After1的系数负向显著

. xtreg y time treated Before3 Before2 Before1 Current After1 After2 After3 i.year,
note: treated omitted because of collinearity
note: 1999.year omitted because of collinearity
Fixed-effects (within) regression              Number of obs   =           70
Group variable: country                       Number of groups  =            7
R-sq:                                         Obs per group:
    within = 0.3885                           min =           10
    between = 0.0116                          avg  =          10.0
    overall = 0.3040                          max  =           10
                                           F(16,47)         =           1.87
                                           Prob > F          =          0.0497
```

y	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
time	1.62e+09	1.40e+09	1.16	0.250	-1.18e+09	4.43e+09
treated	0	(omitted)				
Before3	5.26e+08	2.30e+09	0.23	0.820	-4.10e+09	5.16e+09
Before2	1.94e+09	2.30e+09	0.84	0.404	-2.69e+09	6.57e+09
Before1	-4.53e+08	2.30e+09	-0.20	0.845	-5.08e+09	4.18e+09
Current	-8.06e+08	2.30e+09	-0.35	0.728	-5.44e+09	3.82e+09
After1	-7.15e+09	2.30e+09	-3.10	0.003	-1.18e+10	-2.52e+09
After2	-9.04e+08	2.30e+09	-0.39	0.696	-5.54e+09	3.73e+09
After3	3.21e+08	2.30e+09	0.14	0.890	-4.31e+09	4.95e+09

## • Examples for DID

- ▶ Test Paralled Trend
- ▶ -coefplot-图示

```
. * keep() : 保留关键变量
. * vertical : 转置
. * recast(connect) : 系数连线, 观察动态效果:
. * yline(0) : 增加直线y=0

. coefplot reg, keep(Before3 Before2 Before1 Current After1 After2 After3) ///
    vertical recast(connect) scheme(s1mono) msymbol(circle_hollow) ///
    yline(0, lwidth(vthin) lpattern(dash) lcolor(teal)) ///
    xline(4, lwidth(vthin) lpattern(dash) lcolor(teal)) ///
    ciopts(lpattern(dash) recast(rcap) msize(medium))

. graph export did.png,width(500) replace
(note: file did.png not found)
(file did.png written in PNG format)
```

- Examples for DID

- ▶ Test Paralled Trend

- ▶ `-coefplot-`图示

发现系数在政策前在 0 附近波动，而政策后一年系数显著为负，但很快又回到 0 附近；说明 treatment group 和 control group 可以进行比较，而政策效果可能出现在颁布后一年，随后又很快消失。

